Heat Transfer Near An Ice-Ocean Interface In Supercooled Water

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How does basal hydraulic roughness (drag) differ between ablation and deposition zones?



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What are the thermodynamics of ice growth in the deposition zone?











C. Stevens photo



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Measurements 1 m from interface: $\log(z_0) = -\kappa U / u_*$

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Previous observations of z_0 under undeformed fast ice:

Barrow Strait (NWT, 1995): 0.03 – 0.05 mm Vanmijen Fjord, Svalbard, 2001: hydraulically smooth (~0.01 mm) Freemansundet, Svalbard, 2007: hydraulically smooth (~0.01 mm)



U_* (square root of turbulent stress) from velocity covariance

$$u_{*(\text{cov})} = \left(\left\langle u'w' \right\rangle^2 + \left\langle v'w' \right\rangle^2 \right)^1$$

3-hr average of 15 minute turbulent realizations



*U*_{*} (square root of turbulent stress) from velocity covariance

$$u_{*(\text{cov})} = \left(\left\langle u'w' \right\rangle^2 + \left\langle v'w' \right\rangle^2 \right)^{1/4}$$

3-hr average of 15 minute turbulent realizations



Friction speed from the area-preserving *w* variance spectrum

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$$kS_{ww}(k) = \frac{4}{3}\alpha_{\varepsilon}\epsilon^{2/3}k^{-2/3}$$

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From the covariance estimate:

$$\langle \log(z_0) \rangle = -3.51 \pm 1.04 \quad \Rightarrow \quad \mathbf{z_0} = \mathbf{30} \text{ mm}$$

From the *w* spectral estimate:

 $\langle \log(z_0) \rangle = -3.47 \pm 0.92 \quad \Rightarrow \quad \mathbf{z_0} = \mathbf{31} \, \mathbf{mm}$



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These values are more typical of deformed, multiyear pack, e.g. Arctic Beaufort, Northpole, western Weddell Sea: 30-60 mm, than for undeformed fast ice without platelet growth (~0.01 mm)

Turbulent Heat Flux



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Measure turbulent heat flux:

$$H_{f} = \rho c_{p} \left\langle w'T' \right\rangle$$

Calculate the covariance for each 15 min realization, then average in 3-h bins.



Thermal Balance at the Ice/Ocean Interface



Dimensional analysis: $\langle w'T' \rangle \propto u_* \delta T$ and we find for moderate melting that $H_f \approx \rho c_P c_H u_* [T_{ml} - T_f(S_{ml})]$ where $c_H \sim 0.006$ Dimensional analysis: $\langle w'T' \rangle \propto u_* \delta T$ and we find for moderate melting that $H_f \approx \rho c_P c_H u_* [T_{ml} - T_f(S_{ml})]$ where $c_H \sim 0.006$



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Summary

- McMurdo Sound is an excellent laboratory for studying ice/ ocean interaction in supercooled water
- The persistence of supercooling in the sound suggests that the water column lacks sufficient nucleation sites for extensive frazil production
- Platelet growth appears to increase the hydraulic roughness (drag) of the ice underside compared with more typical undeformed fast ice
- Platelet growth on the ice underside appears to be rate limited by turbulent heat transport away from the boundary, which depends on both u_{*} and ΔT

